Please read these directions before starting your exam.

This is a closed-note exam aside from your one page of notes, double-sided. You may not use any electronic devices to complete this exam, nor can you communicate with anyone besides the proctors and professor. If you are caught cheating, you will receive an F in the course.

For any question, unless specified otherwise, you may use any class without a corresponding import. E.g., if you want to use HashMap, you do not need to also import java.util.HashMap.

Unless otherwise stated, you do not need to spell out the "full design recipe", i.e., write the signature, documentation comments, and tests. Of course, doing so may aid you in your solution.

If you find a mistake, please raise your hand and let one of the proctors know; we will determine whether or not this is the case.

When you are finished, turn in your exam and notes sheet if you have one, then quietly exit.

You have 75 minutes to complete the exam, but it is designed to take only 60 minutes.

Good luck!

Question	Points	Score
1	20	
2	20	
3	20	
4	20	
Total:	80	

Name: ____

IU Email:

Section (Sam/Joshua): ____

- 1. (20 points) Design the computeDiscount(double itemCost, int age, boolean isStudent) method that computes a discount for some item based on their age and student status according to the following criteria:
 - If age < 18, apply a 20% discount.
 - If $18 \le age \le 25$ and they are a student, apply a 25% discount. If they are not a student, do not apply a discount.
 - If $age \ge 65$ and they are a student, apply a 30% discount. If they are not a student, apply a 15% discount.
 - All other cases should not have a discount applied.

Your method should return the total cost of the item after applying the discount. In designing this method, follow the template from class; write the signature, purpose statement, testing, and *then* do the implementation. You should probably use simple numbers for the *itemCost* so you can calculate the discounts in your head. The skeleton code is on the next page.

- 2. (20 points) This question has three parts.
 - (a) (6 points) Design the standard recursive countdown method, which receives an int $n \ge 0$ and returns a String containing a sequence of the even numbers from n down to 0 inclusive, separated by commas.

countdown(10) => "10,8,6,4,2,0"
countdown(23) => "22,20,18,16,14,12,10,8,6,4,2,0"
countdown(0) => "0"

(b) (7 points) Design the countdownTR and countdownTRHelper methods. The former acts as the driver to the latter; the latter solves the same problem as countdown does, but it instead uses tail recursion. Remember to include the relevant access modifiers!

(c) (7 points) Design the countdownLoop method, which solves the problem using either a while or for loop.

3. (20 points) Design the moreThanThree method that, when given an int[] A, returns a new HashSet<Integer> of values containing those values from A that occur strictly more than three times. You cannot use the Stream API. In designing this method, follow the template from class; write the signature, purpose statement, testing, and *then* do the implementation.

```
import static Assertions.assertAll;
import static Assertions.assertEquals;
class MoreThanThreeTester {
    @Test
    void moreThanThreeTest() {
    }
}
import java.util.*; // Import all necessary collections.
class MoreThanThree {
    /***
    *
    *
    *
    *
    */
    ______ moreThanThree(______) {
```

4. (20 points) Oh no! Sam's cat, Marmalade, has scratched part of this exam away and we need you to fix the missing code. Fill in the blanks to complete this generic method implementation. Additionally, write at least two examples where each example uses a different key type. You can write an instance of a LinkedHashMap as $\{<k_1, v_1>, <k_2, v_2>, \ldots, <k_n, v_n>\}$ in your examples to compensate for time.

```
import static Assertions.assertAll;
import static Assertions.assertEquals;
class FindMaxStringTester {
 @Test
 void findMaxStringTest() {
 }
}
import java.util.LinkedHashMap;
class FindMaxString {
 /**
  * Finds the maximum string in a map of some keys
  * of an arbitrary type to strings.
  */
 static _____ findMaxString(LinkedHashMap<____, String> map) {
   String max = "";
   for (____ t : map.keySet()) {
     if (_____) {
       max = map.get(____);
     }
   }
   return max;
 }
}
```

Scratch work

Scratch work